

## §7 Modelling Uncertainty

- probabilistic uncertainty
  - probability of an outcome
  - dice, shuffled cards
  - statistical reasoning
    - Bayesian networks, Dempster-Shafer theory
- possibilistic uncertainty
  - possibility of classifying object
  - *sorites* paradoxes
  - fuzzy sets

## Bayes' theorem

- hypothesis  $H$
- evidence  $E$
- probability of the hypothesis  $P(H)$
- probability of the evidence  $P(E)$
- probability of the hypothesis based on the evidence
$$P(H|E) = (P(E|H) \cdot P(H)) / P(E)$$

## Example

- $H$  — there is a bug in the code
- $E$  — a bug is detected in the test
- $E|H$  — a bug is detected in the test given that there is a bug in the code
- $H|E$  — there is a bug in the code given that a bug is detected in the test



## Example (cont'd)

- $P(H) = 0.10$
- $P(E|H) = 0.90$
- $P(E|\neg H) = 0.10$
- $P(E) = P(E|H) \cdot P(H) + P(E|\neg H) \cdot P(\neg H) = 0.18$
- from Bayes' theorem:
$$P(H|E) = 0.5$$
- conclusion: a detected bug has fifty-fifty chance that it is not in the actual code

## Bayesian networks

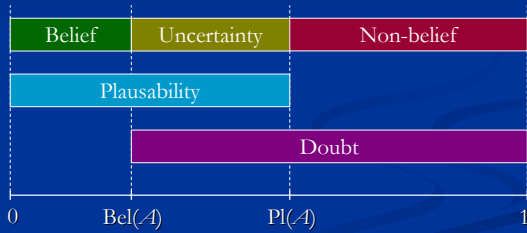
- describe cause-and-effect relationships with a directed graph
  - vertices = propositions or variables
  - edges = dependencies as probabilities
- propagation of the probabilities
- problems:
  - relationships between the evidence and hypotheses are known
  - establishing and updating the probabilities

## Dempster-Shafer theory

- belief about a proposition as an interval  
[belief, plausibility]  $\subseteq [0, 1]$
- belief supporting  $A$ :  $\text{Bel}(A)$
- plausibility of  $A$ :  $\text{Pl}(A) = 1 - \text{Bel}(\neg A)$
- $\text{Bel}(\text{intruder}) = 0.3$ ,  $\text{Pl}(\text{intruder}) = 0.8$ 
  - $\text{Bel}(\text{no intruder}) = 0.2$
  - 0.5 of the probability range is indeterminate



## Belief interval

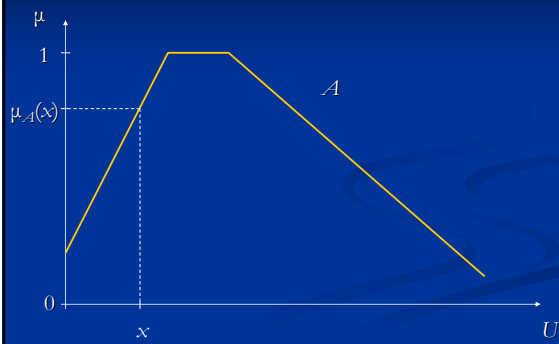


## Fuzzy sets

- element  $x$  has a membership in the set  $A$  defined by a membership function  $\mu_A(x)$ 
  - not in the set:  $\mu_A(x) = 0$
  - fully in the set:  $\mu_A(x) = 1$
  - partially in the set:  $0 < \mu_A(x) < 1$



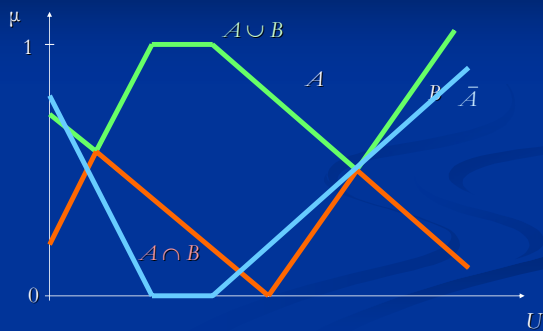
## Membership function



## Fuzzy operations

- union:  $\mu_C(x) = \max\{\mu_A(x), \mu_B(x)\}$
- intersection:  $\mu_C(x) = \min\{\mu_A(x), \mu_B(x)\}$
- complement:  $\mu_C(x) = 1 - \mu_A(x)$
- note: operations can be defined differently

## Fuzzy operations (cont'd)



## Uses for fuzzy sets

- approximate reasoning
- fuzzy constraint satisfaction problem
- fuzzy numbers
- almost any 'crisp' method can be fuzzified!

## Outroduction

- §1 Introduction
- §2 Random Numbers
- §3 Tournaments
- §4 Game Trees
- §5 Path Finding
- §6 Decision-Making
- §7 Modelling Uncertainty

## The intention, huh?

- to provide a glance into the world of computer games as seen from the perspective of a computer scientist









## Examinations

- examination dates (to be confirmed)
  1. October 26, 2005
    - N.B. lecture examination, 12:00–14:00
  2. November 21, 2005
  3. January 30, 2006
- check the exact times and places at <http://www.it.utu.fi/opetus/tentit/>
- remember to enroll! <https://www.it.utu.fi/kurssi-ilmoinen/>

## Examination questions

- questions
  - based on both lectures and lecture notes
  - two questions, à 5 points
  - to pass the examination, at least 5 points (50%) are required
  - grade:  $g = \lceil p - 5 \rceil$
  - questions are in English, but you can answer in English or in Finnish

## My two cents

-  software construction practices: will game programming remain the last reservate for wizards, nerds and geeks?
-  off-the-shelf components: gfx cards, 3d engines, animation tools, audio, AI, networking...
-  mobile platforms: location-based games
-  untapped markets: not every game buyer is (nor even don't want to be) familiar with current game genres
-  independent game publishing: war against apathy!
-  technology breeds new ideas—or does it?