Constraint satisfaction problem

- constraint satisfaction problem (CSP):
 - a set of n variables X
 - a domain D_i for each variable x_i in X
 - a set of constraints restricting the feasibility of the target (u, v) = (v, v) = (v, v)
- tuples (x₀, x₁,..., x_{n-1}) ∈ D₀ × ... × D_{n-1}
 solution: an assignment of value to each variable so that every constraint is satisfied
 - no objective function → not an optimization problem

Example: *n* queens problem as a CSP

- problem: place *n* queens on a *n* × *n* chessboard so that they do not threat one another
- CSP formulation
 - variables: x_i for each row i
 - domain: $D_i = \{ 1, 2, ..., n \}$
 - constraints:
 - $\blacksquare x_i \neq x_j$
 - $x_i x_j \neq i j$ $x_i x_i \neq i j$
 - $= x_j x_i + i j$

Fuzzy constraint satisfaction problem

• fuzzy constraint satiscation problem (FCSP) is a five-tuple $P = \langle V, C_u, W, T, U \rangle$

- V: variables
- U: universes (domains) for the variables
- C_{μ} : constraints as membership functions
- W: weighting scheme
- T: aggregation function

Dog Eat Dog: Modelling the criteria as fuzzy sets

- if the visual observation of the enemy is reliable, then avoid the enemy
- if the visual observation of the prey is reliable, then chase the prey
- if the olfactory observation of the pond is reliable, then go to the pond
- if the visual observation of the enemy is reliable, then stay in the centre of the play field

Dog Eat Dog: Weighting the criteria importances

- fuzzy criterion C_i has a weight $w_i \in [0, 1]$
- a greater value w_i corresponds to a greater importance
- the weighted value from the implication $w_i \rightarrow C_i$
 - classical definition $(A \rightarrow B \Leftrightarrow \neg A \lor B)$: min $\{(1 w_i), C_i\}$
 - Yager's weighting scheme: the weighted membership value:

 $\boldsymbol{\mu}_{C}^{w}(x) = \begin{cases} 1, \text{ if } \boldsymbol{\mu}(x) = 0 \text{ and } w = 0 \\ \\ (\boldsymbol{\mu}_{C}(x))^{w}, \text{ otherwise} \end{cases}$

Dog Eat Dog: Aggregating the criteria

- aggregator should have compensatory properties
- the effect of a poorly satisfied criterion is not so drastic
- mean-based operators instead of conjunction
 ordered weighted averaging (OWA)

Ordered weighted averaging (OWA)

- weight sequence $W = (w_0, w_1, \dots, w_{n-1})^T$ • $\forall w_i \in [0, 1] \text{ and } \Sigma w_i = 1$
- $F(a_0, a_1, \dots, a_{n-1}) = \Sigma w_j b_j$
- b_j is the (j+1)th largest element of the sequence $A = \langle a_0, a_1, \dots, a_{n-1} \rangle$
- by setting the weight sequence we can get $W = \{0, 0, \dots, 1\}$
 - conjunction: W = { 0, 0, ..., 1 } = min{A}
 disjunction: W = { 1, 0, ..., 0 } = max{A}
 - average: $W = \{1/n, 1/n, ..., 1/n\}$
- soft-and operator: $w_i = 2(i+1) / (n(n+1))$
- soft-and operator: $w_i = 2(i + 1) / (n(n + 1))$ • example: n = 4, $W = \{0.1, 0.2, 0.3, 0.4\}$

Outroduction

- §1 Introduction
- §2 Random Numbers
- §3 Tournaments
- §4 Game Trees
- §5 Path Finding
- §6 Decision-Making
- §7 Modelling Uncertainty



Examinations

- examination dates (in Turku)
- 1. October 15, 2007
- 2. November 19, 2007
- 3. December 18, 2007
- check the exact times and places at http://www.it.utu.fi/opetus/tentit/
- remember to enrol!
 https://ssl.utu.fi/nettiopsu/

Examinations (cont'd)

- questions
 - based on both lectures and the textbook
 - two questions, à 5 points
 - to pass the examination, at least 5 points (50%) are required
 - grade: $g = \lfloor p 5 \rfloor$
 - questions are in English, but you can answer in English or in Finnish

Follow-up course: Multiplayer Computer Games

- focus: networking in computer games
- credits: 5 cp (3 cu)
- schedule:
 - October 29 November 29, 2007
 - Mondays 2–4 p.m., Wednesdays 4–6 p.m., and Thursdays 2–4 p.m.
- web page:
 - http://www.iki.fi/smed/mcg

